

S.R DAV Public School Puri  
Diwali Chhath vacation Assignment  
Sub: Mathematics Class - XI

① If  $a \sin \theta + b \cos \theta = a \operatorname{cosec} \theta + b \sec \theta$ ,  
then the expression  $a^2 \cos^6 \theta + b^2 \sin^6 \theta +$   
 $2ab \sin^3 \theta \cos^3 \theta$  equals:

- (a) 1 (b)  $a^2 b^2$  (c) 0 (d)  $ab$

② Both A and B throw a dice. The chance  
the B throws a number not less than  
that thrown by A is

- (a)  $\frac{1}{2}$  (b)  $\frac{21}{36}$  (c)  $\frac{19}{36}$  (d)  $\frac{15}{36}$

③ Find the range of the function  $f$   
defined as  $f(x) = \log_5(3x^2 - 4x + 5)$

④ Given that  $x$  is an integer, find the  
values of  $x$  which satisfy both  $2x + 3 > 7$   
and  $x + 4 < 10$ .

⑤ Evaluate:  $3 \left[ \sin^4 \left( \frac{3\pi}{2} - \alpha \right) + \sin^4 (3\pi + \alpha) \right] -$   
 $2 \left[ \sin^6 \left( \frac{\pi}{2} + \alpha \right) + \sin^6 (5\pi - \alpha) \right]$ .

⑥ Solve the system of inequalities  $2x + 5 \leq 0$ ,  
 $x - 3 \leq 0$

⑦ If  $2 \tan \alpha = 3 \tan \beta$  then find  $\tan(\alpha - \beta)$

- (a)  $\frac{\sin 2\beta}{5 - \cos 2\beta}$  (b) None of these (c)  $\frac{\cos 2\beta}{5 - \cos 2\beta}$  (d)  $\frac{\sin 2\beta}{5 + \cos 2\beta}$

8) mark the correct answer for  $(1+i)^{-1} = ?$

- (a)  $\left(\frac{1}{2} + \frac{1}{2}i\right)$  (b) None of these (c)  $\left(\frac{1}{2} - \frac{1}{2}i\right)$   
(d)  $2-i$

9) Let  $f(x) = \sqrt{x}$  and  $g(x) = x$  be two functions defined in the domain  $\mathbb{R}^+ \cup \{0\}$ .  
Find  $(f-g)(x)$

10) If  $n(A) = 3$  and  $n(B) = 5$  find the maximum number of elements in  $A \cup B$

11) Express  $\frac{(3-2i)(2+3i)}{(1+2i)(2-i)}$  in the form  $a+ib$

12) Solve the linear inequality  $\frac{-3x+10}{x+1} > 0$

13) Three coins are tossed once. Let A denote the event "three heads show", B denote the event "Two heads and one tail show", D denote the event "a head shown on the first coin" and C denote the event "three tails show".  
Which events are (i) mutually exclusive

(ii) simple (iii) Compound.

14) If  $A+B+C = \pi$ , prove that  $\sin^2 \frac{A}{2} + \sin^2 \frac{B}{2} + \sin^2 \frac{C}{2} = 1 - 2 \sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2}$ .

15) Prove:  $4 \sin A \sin(60^\circ - A) \sin(60^\circ + A) = \sin 3A$

16) Evaluate:  $\sin 20^\circ \times \sin 40^\circ \times \sin 60^\circ \times \sin 80^\circ = \frac{3}{16}$

17) The mean and variance of five observations are 6 and 4 respectively. If three of these are 5, 7 and 9. Find the other two observations.